

# TECHBRIEF



U.S. Department of Transportation  
**Federal Highway Administration**

Research, Development, and  
Technology

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Research Center  
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## Development of a Family of Ultra-High Performance Concrete Pi-Girders

FHWA Publication No.: FHWA-HRT-14-028

NTIS Accession No. of the report covered in this TechBrief:  
PB2014-100626

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### Objective

Ultra-high performance concrete (UHPC) is an advanced cementitious composite material, which tends to exhibit superior properties such as exceptional durability, increased strength, and long-term stability. (See references 1–4.) The use of existing structural configurations for materials with advanced properties results in inefficient designs and less cost-effective solutions. Therefore, the purpose of this research is to develop a series of optimized sections of UHPC pi-girders to effectively utilize the superior mechanical properties of UHPC over longer span lengths through finite element analysis (FEA).

### Introduction

The Federal Highway Administration (FHWA) at the Turner-Fairbank Highway Research Center (TFHRC) has executed a research program developing a series of structurally optimized bridge girders that engage the superior mechanical properties of UHPC. Four new, simple span cross-sections were developed based on the pi-girder concept. The research was performed using a calibrated finite element model. The cross-sectional parameters that were varied include girder depth, the bulb width and height, the web thickness, and the strand layout in the bulb. The analysis evaluated the local transverse bending capacity of the deck, the global flexural and shear capacity of the girder, and the live load deflection of the three-girder system. The results indicated that the new cross-sections have enough capacity to accommodate span lengths up to 135 ft (41.1 m). A design chart was developed to facilitate preliminary bridge design.

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## Calibration of Finite Element Model

FEA was used to perform parameter analysis and optimize the cross-section because of its advantages of being efficient and inexpensive. However, the model used in FEA has to be verified against experimental results before it can be expanded for parametric study. Structural tests on a second-generation pi-girder were conducted in the laboratory. A finite element (FE) model based on a concrete damage plasticity model was built and calibrated based on the experimental results.<sup>(5,6)</sup> The results indicated that the FE model can effectively capture the behavior of the tested pi-girders with reasonable accuracy. This makes it possible to conduct parameter analysis and section optimization using the calibrated FE model.

## Deck Thickness

Due to the enhanced mechanical properties of UHPC, the deck thickness tends to be reduced as compared to conventional concrete bridge decks. The thinner deck must be assessed for both local and global performance. In particular, large wheel loads may induce large stresses in the deck, with tensile bending stresses perpendicular to the length of the member. Different deck thicknesses were investigated, along with the influence of diaphragms. A single girder model with short span (15 ft (4.6 m) in this case) was used to suppress global flexure and shear failure. Two wheels were placed adjacent to each other at the center of the deck, creating a 10-inch (0.254-m)-long by 40-inch (1.016-m)-wide area of uniform vertical downward pressure. Diaphragms were applied at both ends, with three diaphragm types being investigated. Table 1 summarizes the maximum wheel load when the principal tensile strain in the UHPC reached the predefined limiting

value of 3,000  $\mu\epsilon$ . The load ratio in the table is defined as the ratio between the maximum applied load that caused the strain to be reached and the wheel load corresponding to Strength I limit state in American Association of State Highway and Transportation Officials. (AASHTO) load and resistance factor design (LRFD).<sup>(7)</sup>

## Global Flexure and Shear Analysis at Maximum Possible Span

To facilitate preliminary bridge design, it is desirable to develop different cross-sections for different span lengths. Across the family of new cross-sections, the slope of certain surfaces and fillet radii were unchanged in order to facilitate the common use of formwork. The increment for girder height was chosen to be 4 inches (102 mm), and the increment in the bulb size (height and width) was 2 inches (51 mm). A single girder model was used to investigate the relationship between cross-section parameters and the span length. The wheel load was applied above the web to suppress artifacts from transverse bending failure. The magnitude of the load corresponds to the standard AASHTO LRFD Strength I wheel load. In the investigation of flexure capacity, the design truck was simulated by applying the entire load of the design truck on the wheel patch at midspan, which is unrealistic but conservative. In the analysis of global shear behavior, the load was applied at a distance of three times the girder depth away from the support point. Through an iterative process, the four cross-sections shown in figure 1 through figure 4 were developed for different spans. More detailed results are summarized in table 2. In the table, the strand layout was named by the number of strands in each row starting from the bottom.

Table 1. Maximum load ratio and equivalent wheel pressure when the strength limit state is reached.

Deck Thickness (inch)	Load Ratio			Wheel Pressure (psi)		
	Stiff Diaphragm	Regular Diaphragm	Soft Diaphragm	Stiff Diaphragm	Regular Diaphragm	Soft Diaphragm
4.5	5.228	4.456	2.251	418	356	180
4.0	4.300	3.840	1.748	344	307	140
3.5	3.428	3.204	1.222	274	256	98

1.0 inch = 25.4 mm  
 1,000 psi = 6.89 MPa

Figure 1. Strand layout of 35-inch (889-mm)-deep section for 80-ft (24.4-m)-span.

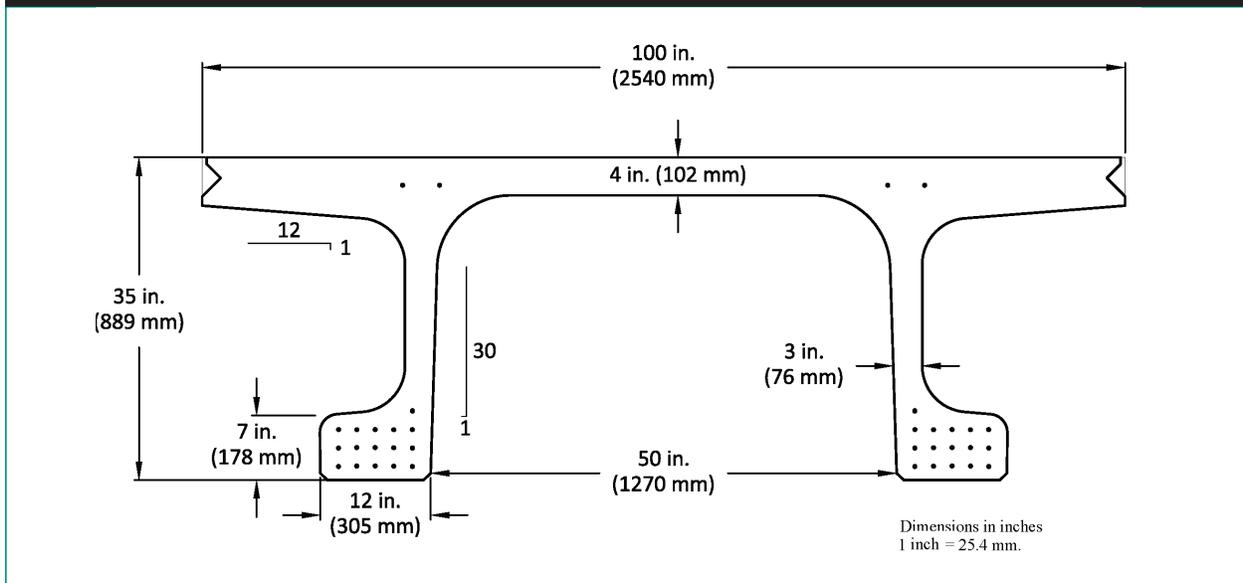


Figure 2. Strand layout of 39-inch (991-mm)-deep section for 95-ft (29-m)-span.

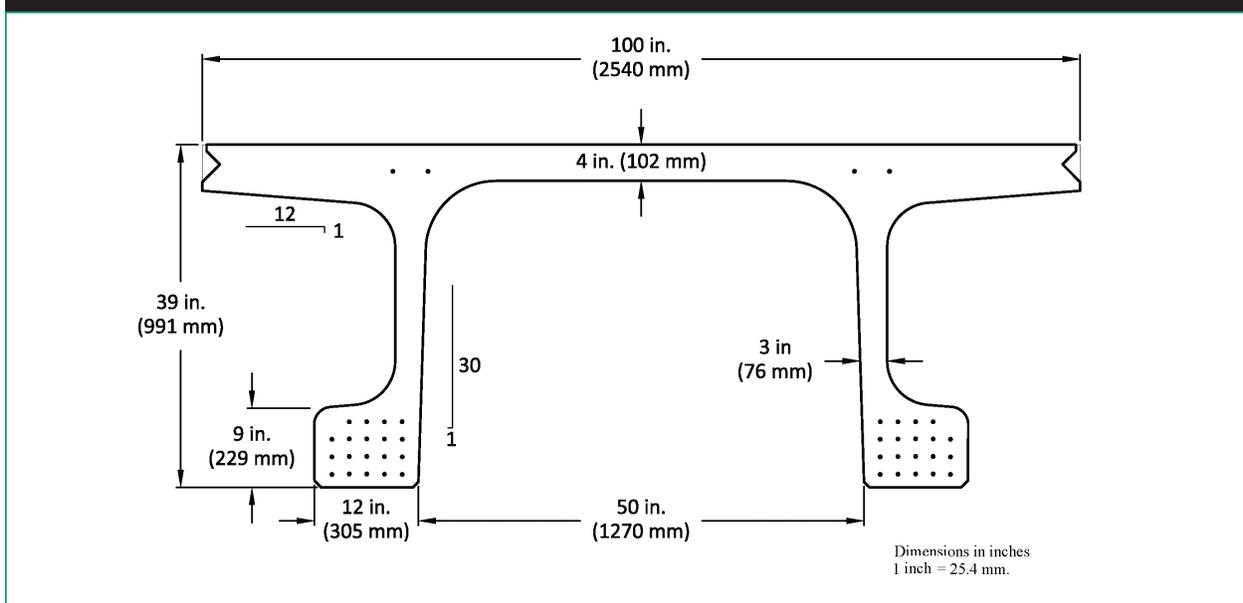


Figure 3. Strand layout of 43-inch (1,092.2-mm)-deep section for 105-ft (32.0-m)-span.

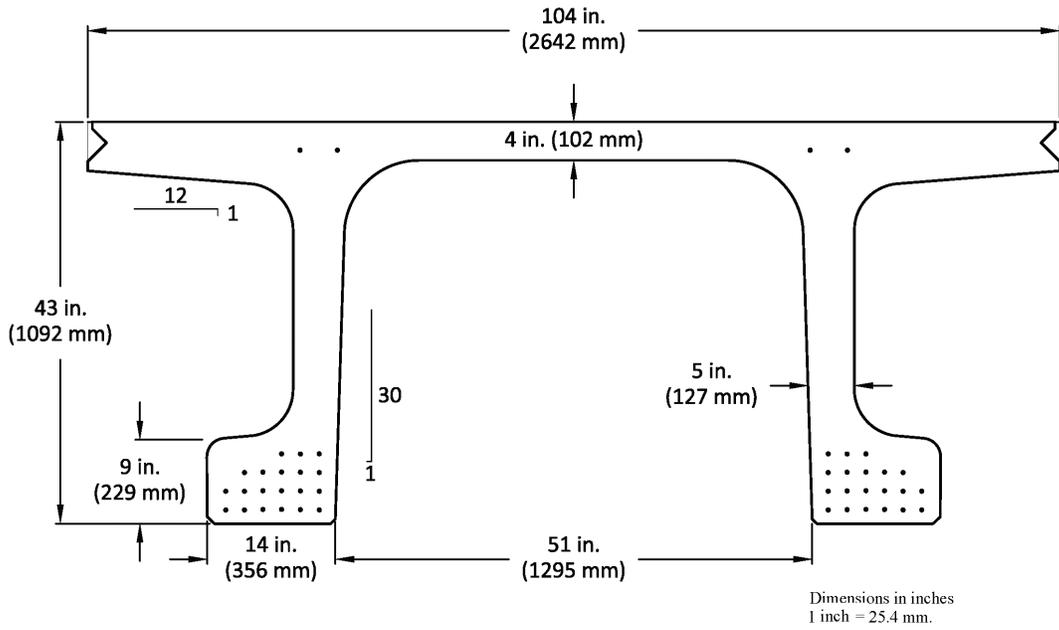
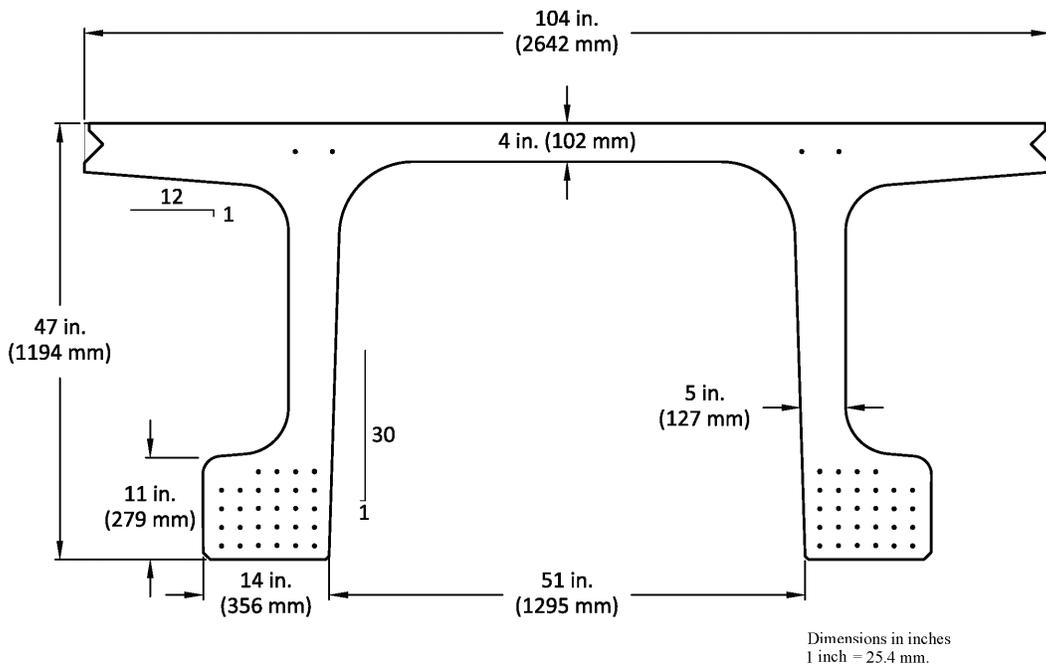


Figure 4. Strand layout of 47-inch (1,193.8-mm)-deep section for 135-ft (41.1-m)-span.



In practice, a bridge span may be shorter than the maximum allowable span for a particular cross-section. To facilitate the use of these research results, shorter spans were also investigated for each cross-section. To achieve this, a parametric analysis was conducted to find the maximum span for cross-sections with the same depth but different strand layouts. The shear capacity was not checked in this

portion of the analysis, as the shear load was basically unchanged. The results of using cross-sections with fewer strands on shorter spans are summarized in table 3. Combining results from previous sections, figure 5 shows a graphic representation of the applicable span range for each girder depth. Table 4 summarizes the properties and applicable span range for each proposed cross-section.

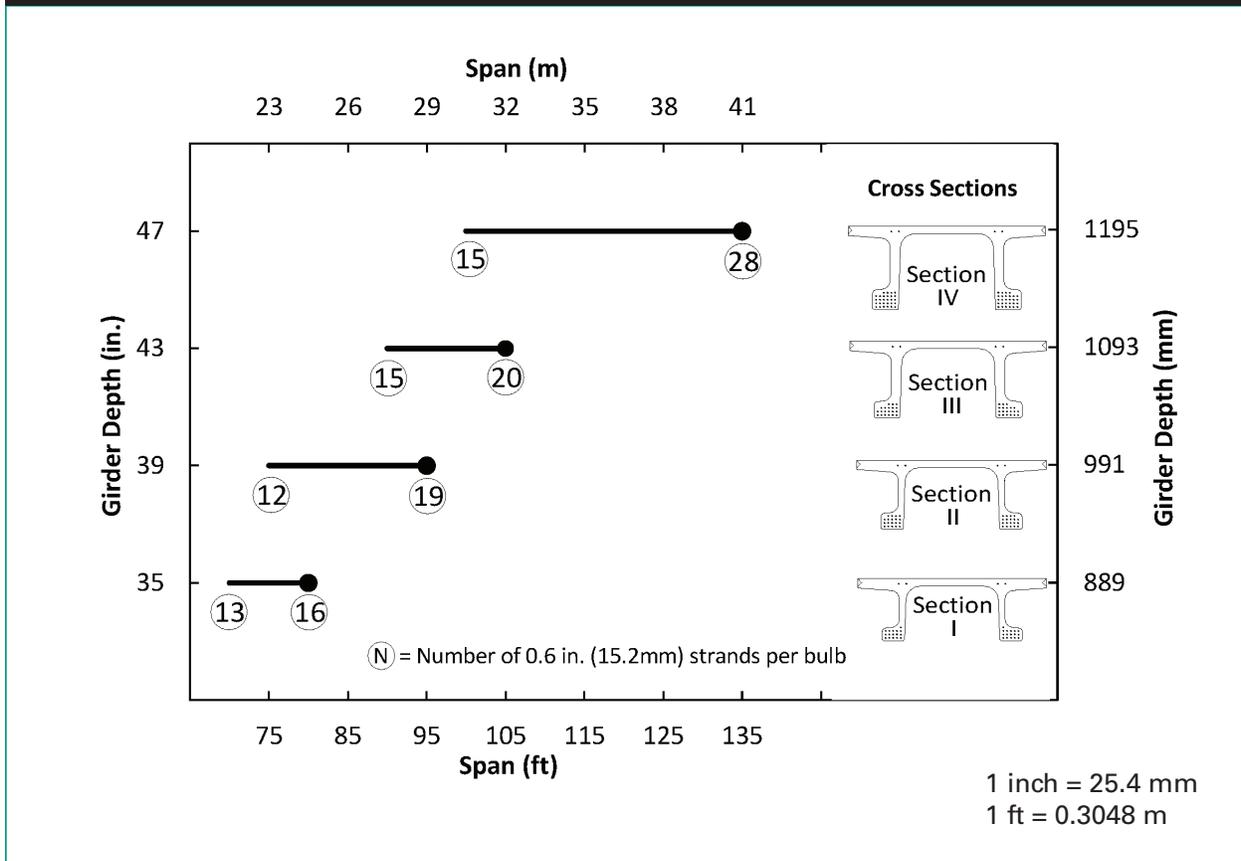
Table 2. Proposed cross-sections for different span length.

Section ID	Section I	Section II	Section III	Section IV
Max. Span (ft (m))	80 (24.4)	95 (29.0)	105 (32.0)	135 (41.1)
Girder depth (inch (mm))	35 (889)	39 (991)	43 (1,092)	47 (1,194)
Deck Width (inch (mm))	100 (2,540)	100 (2,540)	104 (2,642)	104 (2,642)
Web Thickness (inch (mm))	3.37 (85.6)	3.33 (84.5)	5.27 (133.8)	5.23 (132.8)
Bulb Width (inch (mm))	12.03 (305.6)	11.90 (302.3)	13.77 (349.8)	13.63 (346.2)
Bulb Height (inch (mm))	7.25 (184.2)	9.25 (235.0)	9.16 (232.7)	11.25 (285.8)
Strand Layout	5-5-5-1	5-5-5-4	6-6-5-3	6-6-6-6-4
Flexure: Max Tensile Strain at Midspan ( $\mu\epsilon$ )	2,826	2,531	2,520	2,694
Flexure: Max Stress in Strands (ksi (MPa))	251 (1,730)	247 (1,703)	248 (1,710)	250 (1,724)
Shear: Max Tensile Strain in the Web ( $\mu\epsilon$ )	457	291	159	189

Table 3. Modified cross-sections for application on smaller span length.

Section ID	Section I	Section II	Section III	Section IV
Span (ft (m))	70 (21.3)	75 (22.9)	80 (24.4)	100 (30.5)
Strand Layout	5-5-3	5-5-2	6-6-3	6-6-3
Max Flexural Strain at Midspan ( $\mu\epsilon$ )	2,301	2,326	2,273	2,285
Max Stress in Strands (ksi (MPa))	244.0 (1,862)	244.1 (1,863)	243.8 (1,681)	243.7 (1,680)

Figure 5. Summary of developed cross-sections.



## Deflection Analysis

In addition to the strength-limit state, AASHTO LRFD also contains language regarding the flexibility of the structure under live load. It recommends that deflection divided by span not exceed 0.125. The deflection should be taken as the larger of the deflection due to design truck alone or due to 25 percent of the design truck together with the design lane load. Since deflection is primarily driven by span length, the deflection check was conducted only for the maximum span for each cross-section. In this section, a three-girder bridge model was used. The deck widths of the developed cross-sections are 100 inches (2.54 m) or 104 inches (2.64 m). A three-girder system

is enough to accommodate two traffic lanes. This configuration is considered to be conservative compared to other combinations of girder numbers and lane numbers. The lane load and wheel load were biased toward the exterior girder on one side of the bridge. This load pattern creates maximum possible deflection. Trial simulation indicates that the deflection due to truck load is always greater than the deflection due to 25-percent truck load plus design lane load. Therefore, only the deflection under truck load was checked in this section. The results are tabulated in table 4, which shows that all the cross-sections meet the deflection requirements.

Table 4. Section properties and applicable span range for proposed sections.

Section ID	Section I	Section II	Section III	Section IV
Girder Depth (inch)	35	39	43	47
Girder Depth (mm)	889	991	1,092	1,194
Area (inch <sup>2</sup> )	877	935	1,126	1,200
Area (x 10 <sup>4</sup> mm <sup>2</sup> )	56.6	60.3	72.7	77.4
Moment of Inertia (x 10 <sup>9</sup> inch <sup>4</sup> )	1.50	1.84	1.94	2.38
Moment of Inertia (x 10 <sup>14</sup> mm <sup>4</sup> )	6.24	7.66	8.07	9.90
Weight (lb/ft)	944	1,006	1,212	1,291
Weight (kN/m)	13.77	14.69	17.69	18.85
Span Range (ft)	70~80	75~95	80~105	100~135
Span Range (m)	21.3~24.4	22.9~29.0	24.4~32.0	30.5~41.4

Table 5. Deflection under truck loads for refined cross-sections.

Section ID	Section I	Section II	Section III	Section IV
Span (ft (m))	80 (24.4)	95 (29.0)	105 (32.0)	135 (41.1)
Midspan Deflection (inch (mm))	1.13 (28.7)	1.35 (34.3)	1.51 (38.4)	1.98 (50.3)
Deflection/Span (percent)	0.118	0.118	0.120	0.122

## Concluding Remarks

This study conducted a parametric analysis to develop optimized cross-sections using a finite element model calibrated from experimental results. The parameters that were considered in the optimization include deck thickness, girder height, web thickness, bulb size, and strand layouts. The proposed sections were designed to resist loads in excess of those required by the AASHTO LRFD Bridge Design Specifications while meeting the live load deflection recommendations. Even though the deck thickness analysis demonstrated that 3.5-inch (89-mm)

deck is sufficient in terms of strength, a deck thickness of 4 inches (102 mm) is recommended, considering construction tolerances and other uncertainties. A family of UHPC pi-girders was developed for spans ranging up to 135 ft (41.1 m) and loaded under simply supported boundary conditions. Girders with depths of 47 inches (1,194 mm) can be used on spans of 135 ft (41.1 m) or less. Those with 43 inches (1,092 mm), 39 inches (991 mm), and 35 inches (889 mm) can be applied for spans up to 105 ft (32.0 m), 95 ft (29.0 m), and 80 ft (24.4 m), respectively.

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**Key Words**—Ultra-high performance concrete, UHPC, finite element analysis, pi-girder, structural optimization.

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